

**Physics 129 A**  
**Fall 2004**  
**Professor Freedman**  
**October 13, 2004**  
**Problem Set# 6 (Due: October 19, 2004)**  
*(These Problems are taken from Perkins Chapter 3)*

1. Show the reaction  $\pi + d \rightarrow n + n + \pi^0$  cannot occur for pions at rest.
2. What restriction does the decay mode  $K^0 \rightarrow 2\pi^0$  place on (a) the kaon spin (b) the kaon parity?
3. In which isospin states can (a)  $\pi^+ \pi^- \pi^0$ , (b)  $\pi^0 \pi^0 \pi^0$  exist?  
(Hint: First write the isospin wave functions for a pair of pions, and then combine each with the third pion.)
4. State which of the following decays of the  $\rho$  meson ( $J^P = 1^-, I = 1$ ) are allowed by the strong or electromagnetic interaction:

$$\begin{aligned}
 \rho^0 &\rightarrow \pi^+ \pi^- \\
 &\rightarrow \pi^0 \pi^0 \\
 &\rightarrow \eta^0 \pi^0 \\
 &\rightarrow \pi^0 \gamma
 \end{aligned}$$

where the  $\eta$  meson is an isosinglet.

5. The intrinsic parity of the hyperon  $\Xi^0$  with  $S = -2$  can in principle be determined from the observations on capture in hydrogen from an  $S$ -state:

$$\Xi^0 + p \rightarrow \Lambda + \Lambda$$

The polarization of the  $\Lambda$  hyperons produced can be found from the angular asymmetry of the products in the weak decay  $\Lambda \rightarrow p + \pi^-$ . State what is the polarization (if any) of the  $\Lambda$  particles produced in the above reaction and how the relative polarizations are determined from the parity of the  $\Xi^0$ .

6. Both the neutral mesons  $\rho^0(770)$ , with  $J = 1$ , and  $f^0(1275)$ , with  $J = 2$ , decay to  $\pi^+ \pi^-$ . What are their  $C$  and  $P$  parities? State which of the decays  $\rho^0 \rightarrow \pi^0 + \gamma$  and  $f^0 \rightarrow \pi^0 + \gamma$  is or are allowed, and estimate the branching ratio.